

$$y = \alpha_0 + \alpha_1 x + \varepsilon, \quad \hat{y} = \hat{\alpha}_0 + \hat{\alpha}_1 \bar{x},$$

$$\hat{\alpha}_1 = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sum_{i=1}^n (x_i - \bar{x})^2}, \quad \hat{\alpha}_0 = \bar{y} - \hat{\alpha}_1 \bar{x}, \quad t = \frac{r_{xy}}{\sqrt{1 - r_{xy}^2}} \sqrt{n-2} \sim t_{n-2},$$

$$\hat{\mathbf{y}} = \mathbf{X}\hat{\boldsymbol{\alpha}}, \quad \mathbf{e} = \mathbf{y} - \hat{\mathbf{y}} = \mathbf{y} - \mathbf{X}\hat{\boldsymbol{\alpha}}, \quad \hat{\boldsymbol{\alpha}} = (\mathbf{X}'\mathbf{X})^{-1} \mathbf{X}'\mathbf{y},$$

$$\mathbf{D}^2(\hat{\boldsymbol{\alpha}}) = \mathbf{E}(\hat{\boldsymbol{\alpha}} - \boldsymbol{\alpha})(\hat{\boldsymbol{\alpha}} - \boldsymbol{\alpha})' = \sigma^2 (\mathbf{X}'\mathbf{X})^{-1},$$

$$\hat{\sigma}^2 = \frac{1}{n-k-1} \sum_{i=1}^n e_i^2 = \frac{1}{n-k-1} (\mathbf{y}'\mathbf{y} - \hat{\boldsymbol{\alpha}}'\mathbf{X}'\mathbf{y}) = S_e^2,$$

$$1 = R^2 + \varphi^2, \quad R^2 = 1 - \frac{\sum_{i=1}^n e_i^2}{\sum_{i=1}^n (y_i - \bar{y})^2},$$

$$t = \frac{\hat{\alpha}_j}{S_{\alpha_j}} \sim t_{n-k-1}, \quad \hat{\alpha}_j - t_{\alpha} S_{\alpha_j} < \alpha_j < \hat{\alpha}_j + t_{\alpha} S_{\alpha_j},$$

$$Z = \frac{S - \mathbf{E}S}{\sqrt{\mathbf{D}^2 S}} \sim N(0, 1) \quad \mathbf{E}S = \frac{2n_1 n_2}{n_1 + n_2} + 1, \quad \mathbf{D}^2 S = \frac{2n_1 n_2 (2n_1 n_2 - n_1 - n_2)}{(n_1 + n_2)^2 (n_1 + n_2 - 1)},$$

$$r_{xy} = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2 \sum_{i=1}^n (y_i - \bar{y})^2}}$$

$$\hat{\sigma}^2 = \frac{1}{n-1} \sum_{i=1}^n e_i^2, \quad e_i = y_i - \hat{y}_i = y_i - (\hat{\alpha}_0 + \hat{\alpha}_1 x_i).$$